



# Kinematics of Parsec-Scale Jets of Three Gamma-Ray Blazars at 43 GHz: 2013-2018 Behavior

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## Abstract

We analyze the parsec-scale jet kinematics from 2013 January to 2017 December of the gamma-ray bright blazars 4C +21.35 (PKS 1222+216), 3C 279, and PKS 1510-089, monitored roughly monthly with the Very Long Baseline Array (VLBA) at 43 GHz. In a total of 158 images, we measure apparent speeds of 19 emission knots, of which 4 are quasi-stationary. Using the apparent speeds of the components and the timescales of variability from their light curves, we derive the physical parameters of the 15 superluminal knots, including variability Doppler factors, Lorentz factors, and viewing angles. We estimate the half-opening angle of each jet based on the projected opening angle and viewing angle. We calculate the intrinsic brightness temperatures of the cores at all epochs. We finally discuss the changes in jet behavior of these jets compared to their behavior during the time period 2007 June to 2013 January, as described in Jorstad et al. (2017).

## Acknowledgements

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## Jet Structure & Knot Identification

Details of the observations made with the VLBA can be found in Jorstad et al. (2017). We follow the traditional approach to model the total intensity visibility files (e.g., Homan et al. 2001, Jorstad et al. 2001, Jorstad et al. 2017). We represent the total structure of each source at each epoch with a series of 2D Gaussian components that best fit the visibility data determined by iterations with the MODELFIT task in Difmap. The component parameters are flux density,  $S$ , distance with respect to the core,  $R$ , relative position angle (measured north through east),  $\theta_{\text{obs}}$ , and angular size,  $\alpha$ . The brightness temperature,  $T_{\text{b,obs}}$ , is then derived through the method describes in Jorstad et al. 2005. Features are then correlated across epochs by searching for continuity in the fitted parameters. Polynomials of degree  $\ell = 0, 1, \text{ or } 2$  are then fit to the  $X$  and  $Y$  coordinate of each knot, and the best fit is determined by a  $\chi^2$  test. Average parameters for the structure features of the knots for each source are in Table 1 (left), and seen in Fig. 1-3 for 1222+216, Fig. 4-6 for 3C 279, and Fig. 7-9 for 1510-089.

Table 1: Jet Structure

Source	Knot	N	(S) Jy	(R) mas	( $\theta$ ) deg	( $\alpha$ ) mas	Type
1222+216	A0	49	0.63 ± 0.39	0.0	0.0	0.10 ± 0.08	Core
	A1	46	0.26 ± 0.17	0.18 ± 0.05	18.1 ± 18.1	0.05 ± 0.02	St
	A2	45	0.15 ± 0.08	0.45 ± 0.07	11.75 ± 15.1	0.18 ± 0.13	St
	B4	19	0.16 ± 0.06	1.59 ± 0.40	-2.33 ± 0.97	0.33 ± 0.06	M
	B5	24	0.21 ± 0.08	1.10 ± 0.24	15.07 ± 4.63	0.39 ± 0.17	M
	B6	42	0.20 ± 0.10	2.17 ± 0.78	-1.03 ± 1.10	1.04 ± 0.44	M
	B7	13	0.10 ± 0.04	1.72 ± 0.33	4.96 ± 2.35	0.45 ± 0.12	M
	B8	10	0.06 ± 0.02	0.94 ± 0.20	21.20 ± 1.50	0.17 ± 0.04	M
	C33	40	0.33 ± 0.16	0.0	0.0	0.13 ± 0.04	Core
	C34	42	1.84 ± 1.09	0.04 ± 0.08	-158.35 ± 4.72	0.28 ± 0.16	M
3C 279	A0	56	2.05 ± 0.80	0.0	0.0	0.10 ± 0.07	Core
	A1	48	0.35 ± 0.26	0.31 ± 0.09	-28.37 ± 11.35	0.20 ± 0.12	St
	A2	9	0.18 ± 0.09	0.76 ± 0.13	-22.32 ± 4.66	0.42 ± 0.24	St
	B6	6	0.11 ± 0.06	1.36 ± 0.18	-29.56 ± 3.80	0.42 ± 0.22	M
	B7	9	0.19 ± 0.04	0.85 ± 0.41	-33.72 ± 11.11	0.68 ± 0.33	M
	B8	19	0.99 ± 0.59	0.53 ± 0.18	-33.09 ± 6.52	0.32 ± 0.19	M
	B9	17	0.63 ± 0.58	1.42 ± 0.54	-38.70 ± 9.24	0.63 ± 0.39	M
	B10	5	0.12 ± 0.02	0.43 ± 0.10	-33.66 ± 5.11	0.23 ± 0.15	M
	C31	16	0.23 ± 0.08	1.72 ± 0.14	-147.40 ± 1.72	0.27 ± 0.12	M
	C32	16	0.23 ± 0.08	1.72 ± 0.14	-147.40 ± 1.72	0.27 ± 0.12	M
1510-089	A0	56	2.05 ± 0.80	0.0	0.0	0.10 ± 0.07	Core
	A1	48	0.35 ± 0.26	0.31 ± 0.09	-28.37 ± 11.35	0.20 ± 0.12	St
	A2	9	0.18 ± 0.09	0.76 ± 0.13	-22.32 ± 4.66	0.42 ± 0.24	St
	B6	6	0.11 ± 0.06	1.36 ± 0.18	-29.56 ± 3.80	0.42 ± 0.22	M
	B7	9	0.19 ± 0.04	0.85 ± 0.41	-33.72 ± 11.11	0.68 ± 0.33	M
	B8	19	0.99 ± 0.59	0.53 ± 0.18	-33.09 ± 6.52	0.32 ± 0.19	M
	B9	17	0.63 ± 0.58	1.42 ± 0.54	-38.70 ± 9.24	0.63 ± 0.39	M
	B10	5	0.12 ± 0.02	0.43 ± 0.10	-33.66 ± 5.11	0.23 ± 0.15	M
	C31	16	0.23 ± 0.08	1.72 ± 0.14	-147.40 ± 1.72	0.27 ± 0.12	M
	C32	16	0.23 ± 0.08	1.72 ± 0.14	-147.40 ± 1.72	0.27 ± 0.12	M

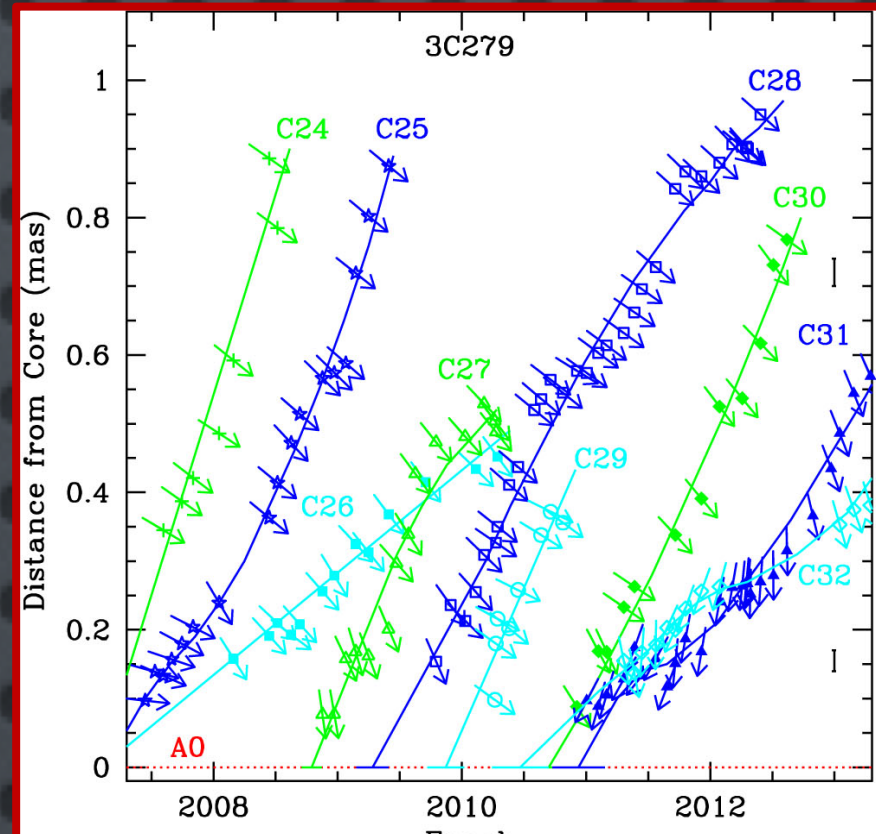
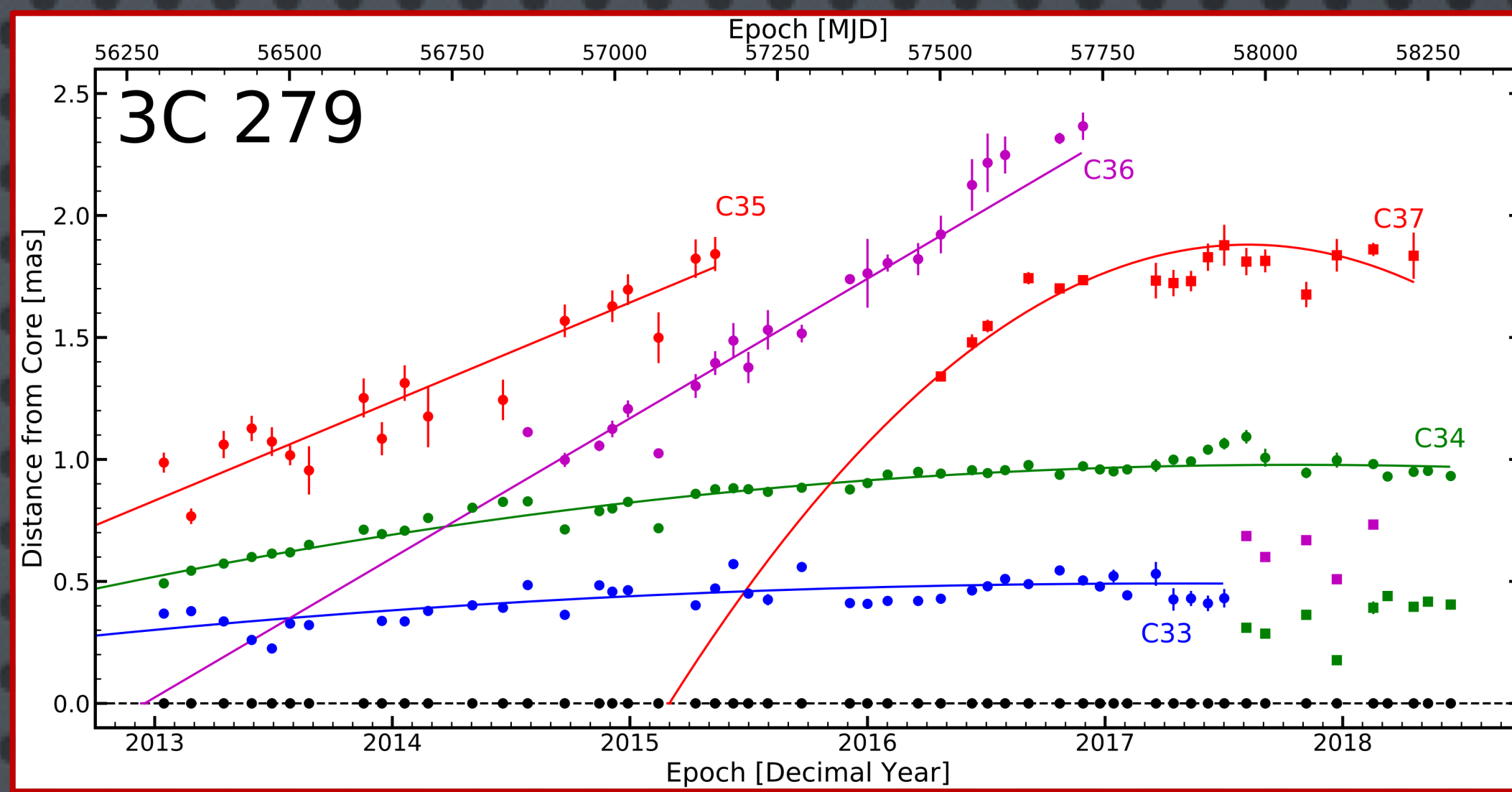


Fig. 1 (above). Sample sequence of VLBA images of the quasar 1222+216. The size of the restoring beam is  $0.16 \times 0.36 \text{ mas}^2$  at a position angle of  $-10^\circ$ . Contours decrease by a factor of  $\sqrt{2}$  w.r.t. the peak flux density across all epochs, 1592 mJy beam<sup>-1</sup> on 2014 November 15. Straight lines across the images show the positions of the core A0 and moving or quasi-stationary knots.

Fig. 2 (above). Separation of jet features from the core of 1222+216 from 2013 Jan. to 2017 Dec. The solid lines or curves represent polynomial fits to the motion, while the dotted line marks the position of the core and quasi-stationary features. Error-bars show the approximate  $1\sigma$  positional uncertainties based on  $T_{\text{b,obs}}$ .

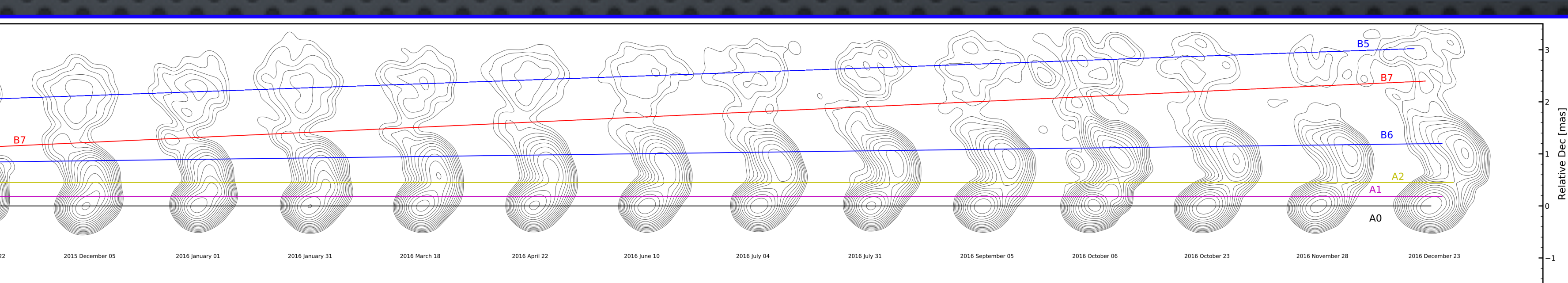


Table 2: Velocities in Jets

Source	Knot	$\ell_x$	$\ell_y$	( $\mu$ ) mas yr <sup>-1</sup>	( $\Phi$ ) deg	( $\beta_{\text{app}}$ ) c	$T_0$ deg
1222+216	B4	1	1	0.631 ± 0.0004	-0.9 ± 0.002	16.75 ± 0.01	2011.88 ± 0.01
	B5	1	1	0.437 ± 0.0002	-36.5 ± 0.03	11.69 ± 0.01	2013.97 ± 0.01
	B6	2	1	0.658 ± 0.0002	-1.4 ± 0.002	17.47 ± 0.01	2012.55 ± 0.01
	B7	1	1	0.938 ± 0.009	-2.6 ± 0.2	24.90 ± 0.24	2015.57 ± 0.02
	B8	2	2	0.751 ± 0.004	-18.4 ± 0.2	19.94 ± 0.11	2016.71 ± 0.02
	C33	1	2	0.046 ± 0.0001	-135.2 ± 0.1	1.46 ± 0.003	2010.55 ± 0.01
	C34	2	2	0.085 ± 0.00001	-134.3 ± 0.01	2.71 ± 0.0003	2010.89 ± 0.1
	C35	1	1	0.406 ± 0.001	-149.3 ± 0.1	12.92 ± 0.03	2010.95 ± 0.01
3C 279	C36	1	1	0.570 ± 0.001	-129.6 ± 0.1	18.14 ± 0.03	2012.96 ± 0.01
	C37	2	2	0.206 ± 0.001	-145.5 ± 0.2	6.56 ± 0.03	2015.17 ± 0.01
	B6	1	1	0.953 ± 0.002	-32 ± 1.1	21.40 ± 0.04	2011.88 ± 0.01
	B7	1	1	1.674 ± 0.011	-23.3 ± 0.4	37.59 ± 0.25	2014.66 ± 0.06
	B8	2	2	0.159 ± 0.112	-1.3 ± 0.5	3.57 ± 2.52	2015.97 ± 0.11
	B9	2	2	1.070 ± 0.003	-27.1 ± 0.3	24.03 ± 0.07	2016.06 ± 0.06
	B10	1	1	1.116 ± 0.026	-34.9 ± 1	25.06 ± 0.58	2018.07 ± 0.02
	C38	13	7	0.70 ± 0.70	1.04 ± 0.59	2.0 ± 0.01	52.9 ± 15.4
1510-089	C39	1.97	0.01	5.92 ± 1.80	3.7 ± 1.2	7.5 ± 3.8	4.6 ± 0.1
	C40	2.02	0.07	13.30 ± 5.04	13.0 ± 2.6	4.3 ± 1.7	4.3 ± 1.7
	C41	1.42	0.02	17.14 ± 8.21	18.2 ± 3.9	3.3 ± 1.5	4.1 ± 2.4
	C42	4.26	0.45	3.21 ± 1.47	8.5 ± 0.5	14.1 ± 2.4	4.1 ± 2.4
	B6	0.40	0.11	37.45 ± 22.15	24.9 ± 14.8	1.3 ± 1.2	1.3 ± 1.2
	B8	0.51	0.01	22.38 ± 13.29	11.5 ± 9.9	0.8 ± 1.1	0.8 ± 1.1
	B9	0.52	0.01	43.21 ± 19.91	28.3 ± 13.4	1.1 ± 0.8	1.1 ± 0.8
	C43	1.97	0.01	5.92 ± 1.80	3.7 ± 1.2	7.5 ± 3.8	4.6 ± 0.1

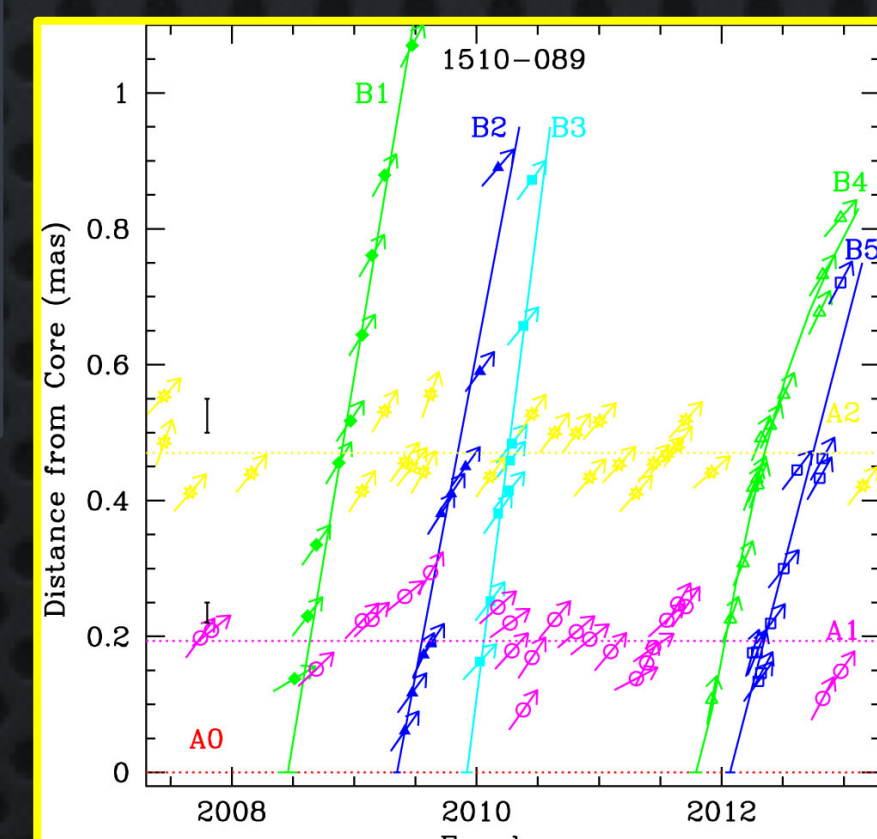
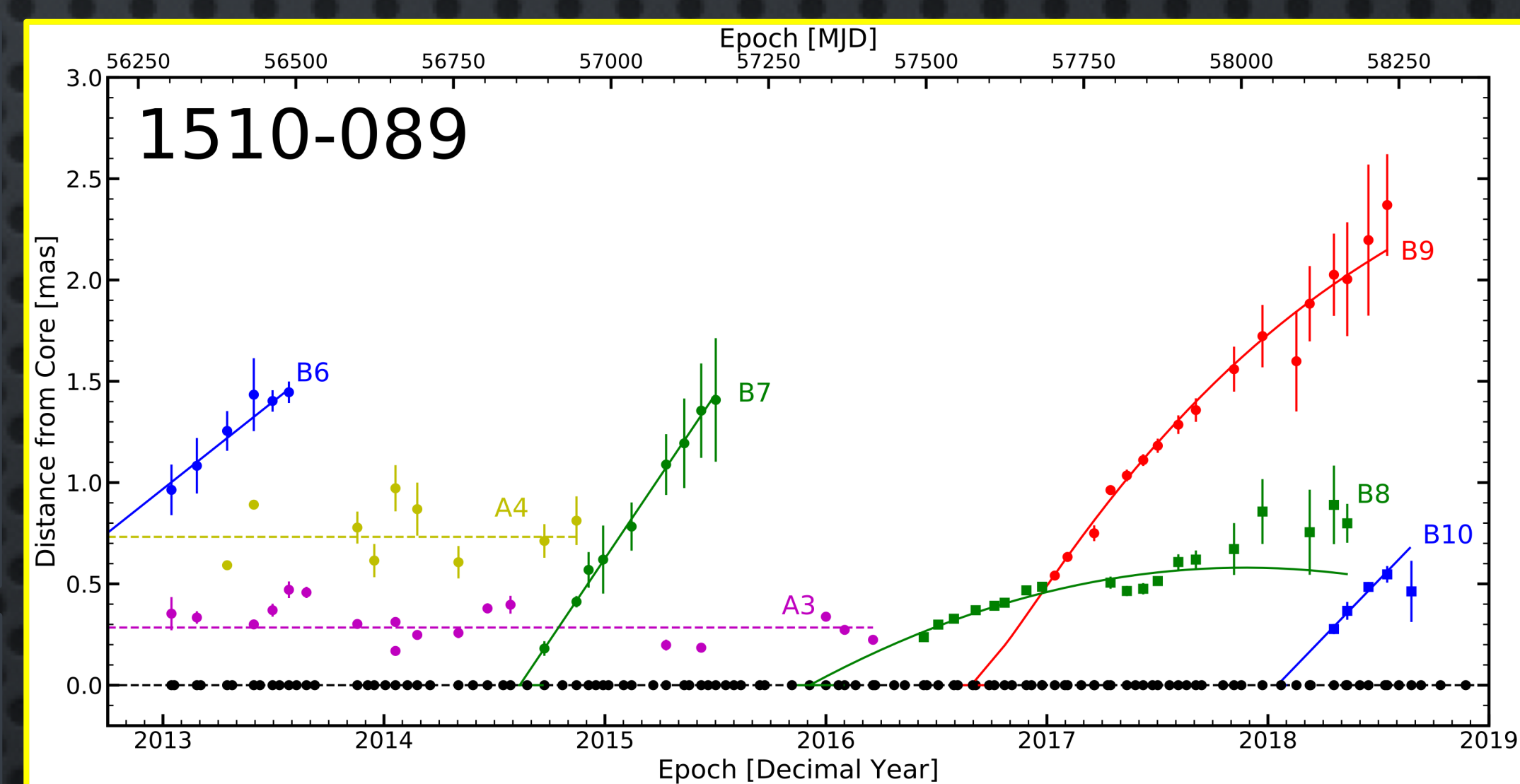


Fig. 4 (above). Sample sequence of VLBA images of the quasar 1510-089. The size of the restoring beam is  $0.19 \times 0.4 \text{ mas}^2$  at a position angle of  $-10^\circ$ . Contours decrease by a factor of  $\sqrt{2}$  with respect to the peak flux density across all epochs, 4277 mJy beam<sup>-1</sup> on 2016 Jan 01. Straight lines across the images show the positions of the core A0 and moving knots.

Fig. 5 (left). The separation of jet features from the core of 1510-089 from mid-2007 to mid-2012 (from Jorstad et al. 2017). The vectors show the P.A. of each knot with respect to the core. The vertical black line segments show the approximate  $1\sigma$  positional uncertainties based on  $T_{\text{b,obs}}$ .

## Knot Kinematics

The name of each knot is a continuation from Jorstad et al. (2017), where “A” knots are quasi-stationary features, “B” knots are moving features, and for 3C 279 the designations have continued from past analyses. Based on the polynomials that best fit the data, we calculate proper motion,  $\mu$ , direction of motion,  $\Phi$ , and apparent speed  $\beta_{\text{app}}$  for each knot, following the method in Jorstad et al. (2005). We then calculate the epoch of ejection  $T_0$  for each knot with statistically significant proper motion. The degree of the fit in each coordinate, average proper motion, direction of motion, apparent speed, and epoch of ejection are provided in Table 2 (upper right).

## Physical Parameters of Jets

Using the kinematics of each knot, we compute physical parameters in the parsec-scale jets of the sources. The average Doppler factor of variability,  $\delta_{\text{var}}$ , is calculated using the formalism developed in Jorstad et al. (2005), using the angular size and timescale of variability,  $\tau_{\text{var}}$ , of each knot and the luminosity distance and redshift of the source. To derive  $\tau_{\text{var}}$ , we make use of the fact that the majority of AGN flares at millimeter wavelengths can be modeled by exponential profiles (Terasanta & Valtaoja 1994; Lister 2001). Thus, we fit a line to the  $\ln(S)$  vs time graph of each knot, and take  $\tau_{\text{var}} = |1/k|$  where  $k$  is the slope of the line. For knots with  $\sigma_{\tau_{\text{var}}} < \tau_{\text{var}}/2$ , we then calculate the Lorentz factor,  $\Gamma$ , and viewing angle,  $\theta_0$ , of each knot using the relations in Jorstad et al. (2017). Values for these parameters can be found in Table 3 (upper right). For each source, we then compute the total average Doppler factor, Lorentz factor, and viewing angle. These are shown in Table 4 (above), along with the maximum intrinsic brightness temperature of the core,  $T_{\text{b,int}}^{\text{core}}$ , intrinsic viewing angle  $\theta_0 = (\max(\theta_0) - \min(\theta_0))/2$ , and number of knots  $N$ .

Table 3: Physical Parameters of Jet Features

Source	Knot	$\tau_{\text{var}}$ years	$\delta_{\text{var}}$	$\Gamma$	$\theta_0$ deg
1222+216	B4	1.92 ± 0.02	6.87 ± 1.25	23.9 ± 0.9	5.9 ± 0.3
	B5	2.47 ± 0.14	6.31 ± 2.77	13.9 ± 0.3	7.6 ± 1.5
	B6	2.09 ± 0.01	19.88 ± 8.41	17.6 ± 4.7	2.6 ± 1.4
	B7	2.47 ± 0.14	7.28 ± 1.98	46.3 ± 4.4	4.2 ± 0.2
	B8	2.33 ± 1.30	2.91 ± 1.76	69.8 ± 19.4	5.6 ± 0.1
	C33	13.7 ± 0.70	1.04 ± 0.59	2.0 ± 0.01	52.9 ± 15.4
	C34	1.97 ± 0.01	5.92 ± 1.80	3.7 ± 1.2	7.5 ± 3.8
	C35	2.02 ± 0.07	13.30 ± 5.04	13.0 ± 2.6	4.3 ± 1.7
3C 279	C36	1.42 ± 0.02	17.14 ± 8.21	18.2 ± 3.9	3.3 ± 1.5
	C37	4.26 ± 0.45	3.21 ± 1.47	8.5 ± 0.5	14.1 ± 2.4
	B6	0.40 ± 0.11	37.45 ± 22.15	24.9 ± 14.8	1.3 ± 1.2
	B8	0.51 ± 0.01	22.38 ± 13.29	11.5 ± 9.9	0.8 ± 1.1
	B9	0.52 ± 0.01	43.21 ± 19.91	28.3 ± 13.4	1.1 ± 0.8
	C38	13.7 ± 0.70	1.04 ± 0.59	2.0 ± 0.01	52.9 ± 15.4
	C39	1.97 ± 0.01	5.92 ± 1.80	3.7 ± 1.2	7.5 ± 3.8
	C40	2.02 ± 0.07	13.30 ± 5.04	13.0 ± 2.6	4.3 ± 1.7
1510-089	C41	1.42 ± 0.02	17.14 ± 8.21	18.2 ± 3.9	3.3 ± 1.5
	C42	4.26 ± 0.45	3.21 ± 1.47	8.5 ± 0.5	14.1 ± 2.4
	B6	0.40 ± 0.11	37.45 ± 22.15	24.9 ± 14.8	1.3 ± 1.2
	B8	0.51 ± 0.01	22.38 ± 13.29	11.5 ± 9.9	0.8 ± 1.1
	B9	0.52 ± 0.01	43.21 ± 19.91	28.3 ± 13.4	1.1 ± 0.8
	C43	13.7 ± 0.70	1.04 ± 0.59	2.0 ± 0.01	52.9 ± 15.4
	C44	1.97 ± 0.01	5.92 ± 1.80	3.7 ± 1.2	7.5 ± 3.8
	C45	2.02 ± 0.07	13.30 ± 5.04	13.0 ± 2.6	4.3 ± 1.7

Table 4: Physical Parameters of Jets

Source	$D$ (Gpc)	( $\delta$ )	( $\Gamma$ )	( $\theta_0$ ) (deg)	$T_{\text{b,int}}^{\text{core}}$ (10 <sup>10</sup> K)	$\theta_0$ (deg)	N
1222+216	2.379	6.6 ± 5.8	24.2 ± 21.0	4.7 ± 1.6	18.15	2.4 ± 1.0	5
3C279	3.080	3.7 ± 6.1	4.9 ± 6	6.6 ± 18.6	74.41	24.8 ± 7.7	5
1510-089	1.919	32.5 ± 8.8	18.5 ± 7.2	1.0 ± 0.2	20.53L	0.3 ± 0.7	3

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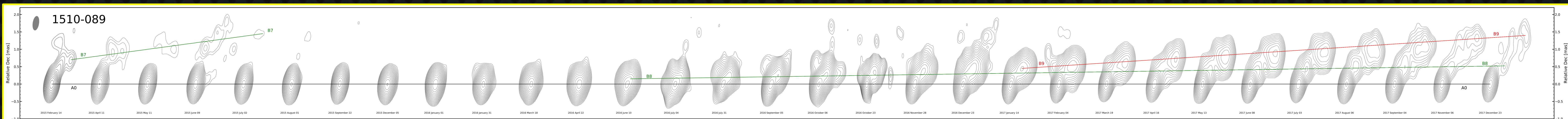


Fig. 6 (right). Sample sequence of VLBA images of the quasar 3C 279. The size of the restoring beam is  $0.15 \times 0.36 \text{ mas}^2$  at a position angle of  $-10^\circ$ . Contours decrease by a factor of  $\sqrt{2}$  with respect to the peak flux density across all epochs, 8386 mJy beam<sup>-1</sup> on 2015 February 14. Straight lines across the images show the positions of the core A0 and moving knots.

Table 5: 2007-2013 Physical Parameters of Jets (from Jorstad et al. 2017)

Source	$D$ (Gpc)	$\langle \delta \rangle$	$\langle \Gamma \rangle$	$\langle \Theta_0 \rangle$ (deg)	$T_{\text{b,int}}^{\text{core}}$ ( $10^{10}$ K)	$\theta_0$ (deg)	N
1222+216	2.379	$7.4 \pm 2.1$	$13.9 \pm 2.1$	$5.6 \pm 1.0$	46.00	$1.5 \pm 1.0$	3
3C279	3.080	$18.3 \pm 1.9$	$13.3 \pm 0.6$	$1.9 \pm 0.6$	82.9	$2.3 \pm 2.2$	3
1510-089	1.919	$35.3 \pm 4.6$	$22.5 \pm 3.3$	$1.2 \pm 0.3$	14.1	$0.5 \pm 0.3$	5